Grade 8 Mathematics EOG (GSE) Quiz Answer Key
Geometry - (MGSE8.G.5 ) Use Informal Arguments

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Score: $\qquad$
1)


Which angle is an EXTERIOR angle?
A) $W$
B) $X$
C) $Y$
D) Z

## Explanation:

Angle $\mathbf{W}$ is exterior, since one of its sides is not a side of the triangle.
2)


Given that lines $L$ and $M$ are parallel, which of the statements is true?
A) $\angle \mathrm{DEF} \cong \angle \mathrm{EBC}$
B) $\angle \mathrm{ABC} \cong \angle D E F$
C) $\angle A B C \cong \angle E B C$
D) $\angle B E F \cong \angle A B C$

## Explanation:

The correct statement is $\angle A B C \cong \angle D E F$. Since lines $L$ and $M$ are parallel angle $A B C$ and angle DEF are alternate exterior angles so the are congruent.


Angle $x$ measures $42^{\circ}$. Find the measure of angle $y$.
A) $42^{\circ}$
B) $48^{\circ}$
C) $138^{\circ}$
D) $148^{\circ}$

## Explanation:

Since both angles make up the sum of the straight line, they are supplementary, or $180^{\circ}$, so $180^{\circ}-42^{\circ}=138^{\circ}$.
4) The angles of a triangle are $2 x, 3 x$, and $4 x$ degrees. Find the value of $x$.
A) 20
B) 30
C) 40
D) 50

## Explanation:

20. The three angles of the triangle add up to 180 degrees. So, $2 x+3 x+4 x=9 x=180$, so $x=20$.
5) 



Given that $\mathrm{j} \| \mathrm{k}$, what is the measure of the missing angle?
A) $30^{\circ}$
B) $40^{\circ}$
C) $60^{\circ}$
D) $120^{\circ}$

## Explanation:

The solution is $60^{\circ}$. Since the angles are on the same side of the transversal, and outside of the two parallel lines, we can conclude that the angles are supplementary. These are sometimes called "same-side exterior angles".
6)

$\angle a$ are $\angle e$ are $\qquad$ angles.
A) perpendicular
B) corresponding
C) complementary
D) alternate interior

## Explanation:

Corresponding angles are formed when two parallel lines are intersected by a third line and they have equal measure.
7)


Find the measure of $\angle \mathrm{x}$.
A) $26^{\circ}$
B) $30^{\circ}$
C) $36^{\circ}$
D) $39^{\circ}$

## Explanation:

$36^{\circ}$

Exterior angles of a triangle supplementary angles (equal $180^{\circ}$ ).
and,
The sum of the three interior angles in a triangle is always $180^{\circ}$.
180-144 = 36
$180-72=108$
then,
$x+36+108=180$
$x+144=180$
$x=36$
8)

$\angle A B C$ and $\angle C B D$ are
A) complementary.
B) supplementary.
C) congruent.
D) vertical.

## Explanation:

Since the angles sum up to $180^{\circ}$, they are supplementary.
9)


## Given: line $a$ is parallel to line $b$

Identify a pair of congruent alternate interior angles.
A) $3 \& 6$
B) $1 \& 8$
C) $2 \& 5$
D) $4 \& 8$

## Explanation:

Angles 3 \& 6 are congruent alternate interior angles. These angles line between the two lines on opposite sides of the transversal.
10)


In the diagram shown, $\angle \mathrm{a}$ and $\angle \mathrm{h}$ are $\qquad$ .
A) vertical angles
B) linear pair angles
C) corresponding angles
D) alternate exterior angles

## Explanation:

The angles are alternate exterior angles. They are angles that lie outside of the two lines on opposite sides of the transversal.
11)

C.


Which diagram shows $\angle 1$ and $\angle 2$ as vertical angles?
A)
B)
C)
D)

## Explanation:

Solution: B. Vertical angles are nonadjacent angles that are formed by intersecting lines. The angles shown in choice C fit this description.
12)


A diagonal support beam is attached to the gate of a fence as shown. Which angles must be congruent in order for the top and bottom sides of the gate to be parallel?
A) $\angle 1$ and $\angle 2$
B) $\angle 3$ and $\angle 4$
C) $\angle 1$ and $\angle 4$
D) $\angle 1$ and $\angle 3$

## Explanation:

The solution is $\angle 1$ and $\angle 4$. These angles are alternate interior angles formed by the transversal and the top and bottom sides of the gate. Angles 2 and 3 are also alternate interior angles, but they are formed by the transversal and the left and right sides of the gate.
13)


Find the measure of $\angle P$.
A) $39^{\circ}$
B) $80^{\circ}$
C) $85^{\circ}$
D) $90^{\circ}$

## Explanation:

$85^{\circ}$

The sum of the three interior angles in a triangle is always $180^{\circ}$.
$P+28+67=180$
$P+95=180$
$P=85$
14)


Line $A B$ is parallel to line $C D$. Which statement is true?
A) Angle d is congruent to angle b.
B) Angle d is congruent to angle c.
C) Angle $d$ is congruent to angle e.
D) Angle $d$ is congruent to angle $f$.

## Explanation:

Angle $\mathbf{d}$ is congruent to angle e because alternate interior angles formed by parallel lines and a transversal are equal.
15)


Angle $b$ and Angle $g$ are known as alternate $\qquad$ angles.
A) consecutive
B) corresponding
C) exterior
D) interior

## Explanation:

Solution: exterior. The two angles lie outside the two lines on opposite sides of the transversal.
16)


If line $L$ is parallel to line $M$, what is true about angle $A B C$ and angle $D E F$ ?
A) They are obtuse.
B) They are congruent.
C) They are supplementary.
D) They are complementary.

## Explanation:

They are congruent because the angles are alternate exterior angles.
17)


Find x and y in the diagram.
A) $x=60, y=30$
B) $x=45, y=60$
C) $x=30, y=60$
D) $x=60, y=120$

## Explanation:

$x=60, y=30$. Since $x$ is part of an equilateral triangle you know that it must be 60 . The vertex angle of the isosceles triangle is 120 . Therefore, y must equal 30 .
18)


Which pair of angles are congruent?
A) 1 and 8
B) 4 and 6
C) 5 and 6
D) 1 and 7

## Explanation:

The solution is 1 and 8 . Angles 1 and 8 are alternate exterior angles formed by parallel lines and a transversal. Therefore, these angles are congruent.
19) $\triangle A B C$ is isosceles. If $m \angle A=100^{\circ}, m \angle B=(12 x+4)^{\circ}$, and $m \angle C=(14 x-2)^{\circ}$, find $x$.
A) 1
B) 3
C) 5
D) 7

## Explanation:

You did not need to know $m \angle A$ to solve this problem. Set $12 x+4$ and $14 x-2$ equal to each other and solve. The correct answer is $x$ $=3$.
20)


Which lines are parallel?
A) $\quad p$ and $q$
B) $q$ and $r$
C) $\quad p$ and $s$
D) $r$ and $s$

## Explanation:

The solution is $p$ and $s$. Since $111^{\circ}$ and $69^{\circ}$ are supplementary we can conclude that lines $p$ and $s$ are parallel.
21)


Given: $\angle 1 \cong \angle 8$

Which lines must be parallel?
A) $r$ and $s$
B) $\quad p$ and $q$
C) $\quad p$ and $r$
D) $\quad q$ and $s$

## Explanation:

The solution is $\boldsymbol{p}$ and $\boldsymbol{q}$. Since angles 1 and 8 are congruent alternate exterior angles and r is the transversal, we can conclude that lines $p$ and $q$ are parallel.
22)


Determine which lines in the diagram are parallel.
A) $a \| b$
B) $b \| c$
C) $a \| c$
D) $\quad b \| d$

## Explanation:

The solution is $\boldsymbol{a} \| \boldsymbol{c}$. Lines $a$ and $c$ both have a slope of 2 . Therefore, the lines are parallel.
23)


If $\triangle A B C$ is similar to $\triangle D E F$, the $m \angle A=50^{\circ}$, and $m \angle E=70^{\circ}$, what is $m \angle C$ ?
A) $60^{\circ}$
B) $70^{\circ}$
C) $90^{\circ}$
D) $120^{\circ}$

## Explanation:

$60^{\circ}$ is the correct answer.
Since $\triangle A B C$ is similar to $\triangle D E F$, the $m \angle E=m \angle B=70^{\circ}$.
We're given that $\mathrm{m} \angle \mathrm{A}=50^{\circ}$.
The sum of the angles in a triangle is $180^{\circ}$,
so $m \angle C=180-70-50=60^{\circ}$


Determine which statement is true.
A) $\quad t \| u$ and $v \| w$
B) $\quad t \| w$ and $u \| v$
C) $\quad t \| v$ and $u \| w$
D) $\quad t \| u$ and $u \| v$

## Explanation:

The solution is $t \| v$ and $u \| \boldsymbol{w}$. Since $60^{\circ}$ and $120^{\circ}$ are supplementary, this allows us to conclude that lines $t$ and $v$ are parallel. Also, since $70^{\circ}$ and $110^{\circ}$ are supplementary we can conclude that lines $u$ and $w$ are parallel.
25)


## Given: line $a$ is parallel to line $b$

Identify a pair of congruent corresponding angles.
A) $1 \& 4$
B) $1 \& 8$
C) $2 \& 5$
D) $4 \& 8$

## Explanation:

Angles 4 \& 8 are congruent corresponding angles. These angles occupy corresponding positions on the same side of the transversal. Since the lines are parallel, we can conclude that these angles are congruent.
26)


> Greg and Lu are building a toy hydraulic crane, as shown in the picture.

What is $\mathrm{m} \angle \mathrm{ABC}$ ?
A) $100^{\circ}$
B) $115^{\circ}$
C) $120^{\circ}$
D) $135^{\circ}$

Explanation:
$135^{\circ}$
The sum of the angles of any triangle is $180^{\circ}$.
In $\triangle \mathrm{ABC}, 20^{\circ}+25^{\circ}+\angle \mathrm{ABC}=180^{\circ}$
$\rightarrow \angle \mathrm{ABC}=180^{\circ}-20^{\circ}-25^{\circ}=135^{\circ}$
27)


A carpenter designs an A-frame chalkboard. Its support bars form the legs of an isosceles triangle.
If the measure of base angle $A B C$ is $75^{\circ}$, what is $m \angle B A C$ ?
A) $15^{\circ}$
B) $30^{\circ}$
C) $75^{\circ}$
D) $105^{\circ}$

## Explanation:

The base angles of an isosceles triangle are equal, so $\mathrm{m} \angle \mathrm{ACB}=75^{\circ}$.
The sum of the angles of any triangle is $180^{\circ}$.
$75^{\circ}+75^{\circ}+\mathrm{m} \angle \mathrm{BAC}=180^{\circ}$
$m \angle B A C=180^{\circ}-\left(75^{\circ}+75^{\circ}\right)=30^{\circ}$
28)


Given that lines $a$ and $b$ are parallel and that $\mathrm{m} \angle 6=65^{\circ}$, find $\mathrm{m} \angle 3$.
A) $40^{\circ}$
B) $65^{\circ}$
C) $115^{\circ}$
D) $135^{\circ}$

## Explanation:

$65^{\circ}$ is correct. $\mathrm{m} \angle 6$ and $\mathrm{m} \angle 3$ are alternate interior angles. The pairs of angles on opposite sides of the transversal but inside the two lines are alternate interior angles. Alternate interior angles of parallel lines cut by a transversal are congruent.
29)


Find the measure of $\angle S M K$.
A) $36^{\circ}$
B) $48^{\circ}$
C) $56^{\circ}$
D) $66^{\circ}$

## Explanation:

66

Exterior angles of a triangle supplementary angles (equal $180^{\circ}$ ).
and,
The sum of the three interior angles in a triangle is always $180^{\circ}$.
$x+30+36=180$
$x+66=180$
$x=114$
then,
$180-114=66$
Also, the exterior angle is equal to the sum of the two remote interior angles.
$30+36=66$
30)


Find the measure of $\angle D F G$.
A) $24^{\circ}$
B) $34^{\circ}$
C) $58^{\circ}$
D) $62^{\circ}$

## Explanation:

Exterior angles of a triangle supplementary angles (equal $180^{\circ}$ ).
and,
The sum of the three interior angles in a triangle is always $180^{\circ}$.
$x+24+34=180$
$x+58=180$
$x=122$
then,
$180-122=58$
Also, the exterior angle is equal to the sum of the two remote interior angles.
$24+34=58$

